

Sec. 10.1 Adding & Subtracting Polynomials

Standard Form:

Terms are placed in descending order, from largest degree to smallest degree

Example: $2x^3 + 5x^2 - 4x + 7$

Degree of each term is the exponent of the variable.

Degree of a polynomial is the largest degree of its terms

Leading Coefficient is the coefficient of the first term when the polynomial is written in standard form.

Examples:

Rewrite the polynomial in standard form, then identify the coefficients.

1. $-4x^2 + x^3 + 3$

2. $4 - x + 2x^2$

Classifying Polynomials:

<u>Number of terms</u>	<u>Name</u>
One	monomial
Two	binomial
Three	trinomial

Examples

<u>Polynomial</u>	<u>Degree</u>	<u>Classified by Degree</u>	<u>Classified by # of terms</u>
6			
-2x			
3x + 1			
$-x^2 + 2x - 5$			
$4x^3 - 8x$			
$2x^4 - 7x^3 - 5x + 1$			

Adding & Subtracting Polynomials

To add or subtract polynomials, add or subtract like terms.

Examples:

1. $(5x^3 - x + 2x^2 + 7) + (3x^2 + 7 - 4x) + (4x^2 - 8 - x^2)$

2. $(2x^2 + x - 5) + (x + x^2 + 6)$

3. $(-2x^3 + 5x^2 - x + 7) - (-2x^3 + 3x - 4)$

4. $(x^2 - 8) - (7x + 4x^2)$

5. $(3x^2 - 5x + 3) - (2x^2 - x - 4)$

6. $(8x^2 - 2x + 4) + (4x^2 - 1 - 3x^3)$

10-1 Algebra

Identify the leading coefficient, classify by degree and by number of terms.

$$25) \quad -\frac{2}{3}x + 5x^4 - \frac{5}{6}$$

Coeff. Degree #

$$27) \quad -9t^2 + 3t^3 - 4t^4 - 15$$

Coeff. Degree #

Add or subtract the polynomials.

$$41) \quad (x^3 + x^2 + 1) - x^2$$

$$45) \quad (6b^4 - 3b^3 - 7b^2 + 9b + 3) + (4b^4 - 6b^2 + 11b - 7)$$

$$47) \quad (9x^3 + 12) + (16x^3 - 4x + 2)$$

$$55) \quad (6t^2 - 19t) - (3 - 2t^2) - (8t^2 - 5)$$

$$59) \quad (9x^4 - x^2 + 7x) + (x^3 - 6x^2 + 2x - 9) - (4x^3 + 3x + 8)$$

$$61) \quad (-3.8y^3 + 6.9y^2 - y + 6.3) - (-3.1y^3 + 2.9y - 4.1)$$

Use the distributive property to simplify the expression.

73) $-3(x + 1) - 2$

75) $11x + 3(8 - x)$

77) $-4(1 - x) + 7$

Practice A

For use with pages 576–582

Write the polynomial in standard form.

1. $3x + 4x^2 - 5$

2. $5x^2 + 4 - 3x$

3. $x - 7x^3 + 2$

4. $8 + 2x + 4x^2$

5. $5x^2 + 4x^3 - 2x$

6. $-4x + 7x^4 - 5x^3 + 1$

7. $3x - 7 + 2x^2$

8. $7x - 2$

9. $-x + 2x^2 + x^3 - 2$

Identify the leading coefficient, and classify the polynomial by degree and by number of terms.

10. 14

11. $2x + 3$

12. $-3x^2 + 6x - 2$

Leading Coefficient			
Degree			
Number of Terms			

13. $x^3 - 5$

14. $1 - x^4$

15. $x^2 + 4x - x^4 + 3x^3 - 8$

Leading Coefficient			
Degree			
Number of Terms			

Use a vertical format to add or subtract.

19. $(x^2 + 2x + 7) + (4x^2 + x - 3)$

20. $(5x^2 - 2x + 4) + (-2x^2 + 3x - 1)$

$$21. (5n^2 + 2n + 3) - (n + 2)$$

$$22. (6n^2 + 4n + 6) - (5n^2 + n + 2)$$

$$23. (2a^3 - 4a^2 + 7) + (-2a^2 + a - 3)$$

$$24. (4n^2 - 6n + 5) - (8n^2 + n + 3)$$

Use a horizontal format to add or subtract.

$$25. (x^2 + 2x + 1) + (x - 3)$$

$$26. (3m^2 + 2m + 1) - (-2m^2 + 4m)$$

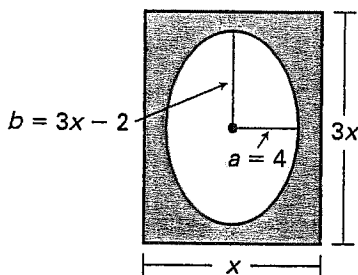
$$27. (7x + 1) - (-x^2 + 3x - 5)$$

$$28. (5x^2 - 9) + (-3x^2 + 5x + 9)$$

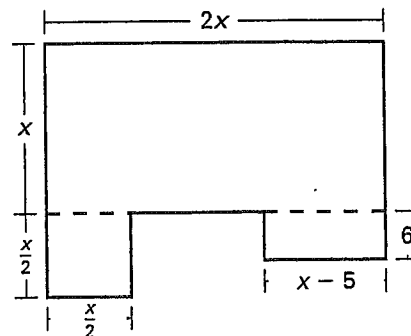
$$29. (7x^3 - 8x^2 + 4) + (9x^2 + 5x + 2)$$

$$30. (n^2 - 2n) - (-5n^2 + 3n - 1)$$

37. **Photograph Mat** A mat in a frame has an opening for a photograph (see figure). Find an expression for the area of the mat. (Area of opening: $A = \pi ab$).



38. **Floor Plan** The first floor of a home has the floor plan shown below. Find an expression in standard form for the area of the first floor.



Sec. 10.2 Multiplying Polynomials
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Match each area to the correct model. Then use the model to find the product.

1. $x(x)$

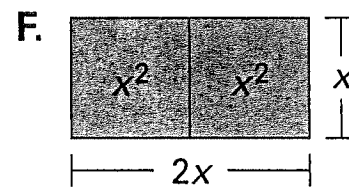
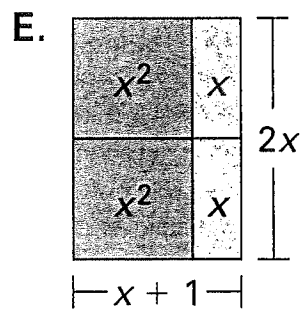
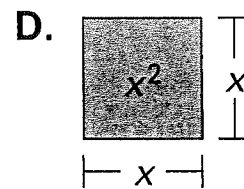
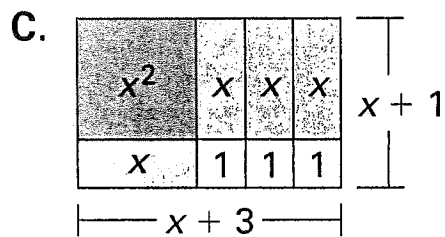
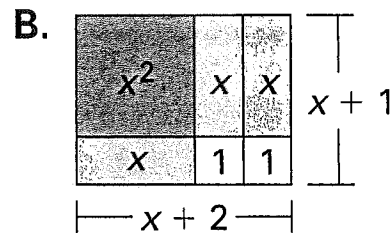
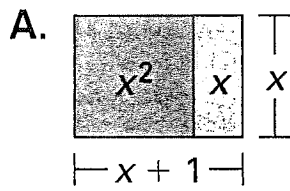
2. $x(x + 1)$

3. $2x(x)$

4. $2x(x + 1)$

5. $(x + 2)(x + 1)$

6. $(x + 3)(x + 1)$



Algebra

Name _____

Date _____ Hour _____

Sec. 10.2 Multiplying Polynomials

Examples:

Multiply:

1. $5(2x^2 - 3x - 4)$

2. $-6(5 - 2x - x^3)$

3. $(x + 2)(x - 3)$

FOIL

When multiplying two binomials, a method called FOIL can be used.

Multiply the **F**irst, **O**uter, **I**nnner, and **L**ast terms

4. $(3x + 4)(x + 5)$

5. $(2x + 3)(x - 3)$

6. $(2x - 3)(x - 2)$

7. $(4x - 7)(2x - 5)$

8. $(x - 2)(5 + 3x - x^2)$

9. $(x - 4)(5x + 9 - 2x^2)$

10. $(4x^2 - 3x - 1)(2x - 5)$

11. $(5x^2 - x - 3)(6x - 5)$

12. $(2x - 1)(3x^2 - x - 4)$

13. $(4x^3 - 2x + 5)(2x^2 - x + 1)$

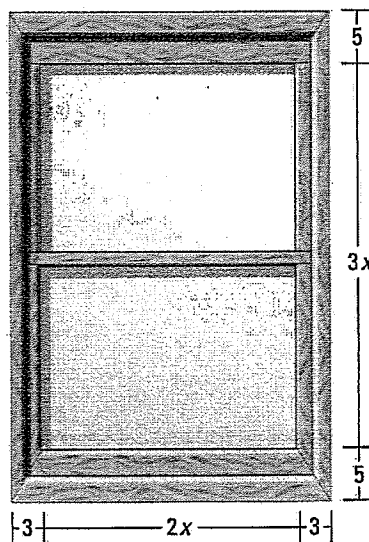
14. $(4x - 1)(5 - 3x)$

15. $(x + 6)(x - 6)$

16.

The diagram at the right shows the basic dimensions for a window. The glass portion of the window has a height-to-width ratio of 3 : 2. The framework adds 6 inches to the width and 10 inches to the height.

- a. Write a polynomial expression that represents the total area of the window, including the framework.
- b. Find the area when $x = 10, 11, 12, 13,$ and $14.$



x (in)	A (in ²)
10	
11	
12	
13	
14	

SOLUTION

10-2 Algebra**Pages 587-589**

Find the product.

42) $(3x + 4)\left(\frac{2}{3}x + 1\right)$

47) $(-4s^2 + s - 1)(s + 4)$

Simplify.

63) $\left(\frac{1}{3}m\right)^2$

65) $(0.5w)^2$

67) $(4^2)^4$

69) $(4c^2)^4$

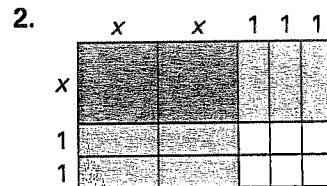
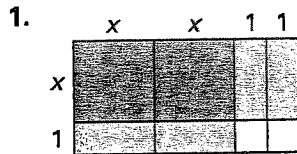
71) $(-w^4)^3$

73) $(8x^2y^8)^3$

Practice A

For use with pages 584–589

Write an equation that represents the product of two binomials as shown in the area model.



Find the product.

3. $2(3x + 1)$

4. $-4(3x - 5)$

5. $(2x)(5x - 1)$

6. $6n(4 - 5n)$

7. $x^2(3x - 7)$

8. $(8m^2 - 4m + 1)(3m^2)$

9. $(-5t)(t^2 + 2t - 4)$

10. $3x^2(2x^2 - 4x - 7)$

11. $(5a^2 + 3a - 7)(-2a^2)$

Use the distributive property to find the product.

12. $(t + 3)(t + 3)$

13. $(n + 5)(n + 1)$

14. $(2x + 5)(x - 4)$

15. $(4a + 5)(2a - 3)$

16. $(3x^2 + 2x + 1)(x + 3)$

17. $(4x^2 - 3x + 2)(2x + 5)$

Use the FOIL pattern to find the product.

18. $(w + 5)(w + 2)$

19. $(3z + 1)(z + 2)$

20. $(x - 2)(x - 3)$

21. $(4x + 7)(x + 5)$

22. $(2x - 2)(x + 8)$

23. $(5n + 3)(4n - 2)$

Find the product.

24. $(3b - 2)(2b - 3)$

25. $(5x + 4)(3x - 2)$

26. $(10n + 5)(3n - 2)$

27. $(x - 7)(3x + 9)$

28. $(4t + 3)(4t + 3)$

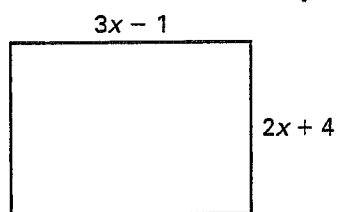
29. $(x^2 + 3x + 1)(x - 2)$

Find an expression for the area of the figure. Give your answer as a quadratic polynomial.

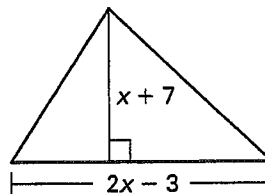
$$A = lw$$

$$A = \frac{1}{2}bh$$

30.



31.



Sec. 10.3 Special Products of Polynomials
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Use FOIL to find the patterns in each group

Group A

$(x-2)(x+2)$

$(2n+3)(2n-3)$

$(x+y)(x-y)$

Group B

$(x+3)^2$

$(5x+2)^2$

$(x+y)^2$

Group C

$(y-2)^2$

$(3p-7)^2$

$(x-y)^2$

SPECIAL PRODUCT PATTERNS**SUM AND DIFFERENCE PATTERN**

$(a+b)(a-b) = a^2 - b^2$

Example: $(3x-4)(3x+4) = 9x^2 - 16$

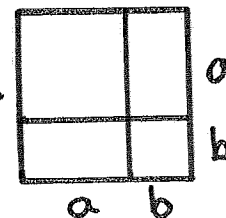
SQUARE OF A BINOMIAL PATTERN

$(a+b)^2 = a^2 + 2ab + b^2$

Example: $(x+4)^2 = x^2 + 8x + 16$

$(a-b)^2 = a^2 - 2ab + b^2$

Example: $(2x-6)^2 = 4x^2 - 24x + 36$



Examples:

Find the products:

1. $(5t - 2)(5t + 2)$

2. $(7x - 4)(7x + 4)$

3. $(3x + 4)^2$

4. $(2x - 7y)^2$

5. $(2p - 5q)^2$

6. $(4x - 10)(4x + 10)$

7. $(3s - 5t)(3s + 5t)$

8. $(6x - 5)^2$

10-3 Algebra **Pages 590-595**
Special Product Patterns
Sum and Difference Pattern

$$(a + b)(a - b) =$$

Example

$$(3x - 4)(3x + 4) =$$

Square of a Binomial Pattern

$$(a + b)^2 =$$

Example

$$(x + 4)^2 =$$

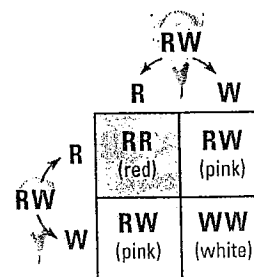
$$(a - b)^2 =$$

Example

$$(2x - 6)^2 =$$

Modeling a Punnett Square

The Punnett square at the right is an area model that shows the possible results of crossing two pink snapdragons, each with one red gene R and one white gene W . Each parent snapdragon passes along only one gene for color to its offspring. Show how the square of a binomial can be used to model the Punnett square.



Each parent snapdragon has half red genes and half white genes.

Simplify the expression. (no negative exponents)

63) $\left(\frac{x}{4}\right)^3$

65) $\left(\frac{4x}{y^3}\right)^3$

67) $\frac{3x^2y}{2x} \cdot \frac{6xy^2}{y^3}$

Solve the equation algebraically.

75) $x^2 - 10 = 6$

77) $\frac{1}{5}x^2 = 5$

79) $\frac{2}{3}x^2 = 6$

Practice A

For use with pages 590–596

Find the missing term.

1. $(x - y)^2 = x^2 - \underline{\hspace{1cm}} + y^2$

2. $(a + b)^2 = a^2 + \underline{\hspace{1cm}} + b^2$

Write the product of the sum and difference.

7. $(x + 2)(x - 2)$

8. $(t + 3)(t - 3)$

9. $(x + 9)(x - 9)$

10. $(5 + c)(5 - c)$

11. $(n + 5)(n - 5)$

12. $(2x + 7)(2x - 7)$

13. $(7 + d)(7 - d)$

14. $(3x + 1)(3x - 1)$

15. $(5x + 3)(5x - 3)$

Write the square of the binomial as a trinomial.

16. $(x + 4)^2$

17. $(x - 5)^2$

18. $(x + 8)^2$

19. $(2t + 3)^2$

20. $(3y - 5)^2$

21. $(4m - 3)^2$

22. $(2m + 4)^2$

23. $(2y + 9)^2$

24. $(2k - 3)^2$

Find the product.

25. $(w + 5)(w - 5)$

26. $(3z + 1)(3z - 1)$

27. $(x - 2)(x + 2)$

28. $(4x + 3)(4x - 3)$

29. $(2x - 9)(2x + 9)$

30. $(5n + 1)^2$

31. $(x - 5)^2$

32. $(3x - 2)^2$

33. $(7b + 3)^2$

Use mental math to find the product.

34. $18 \cdot 22$

35. $27 \cdot 33$

36. $54 \cdot 46$

37. **Blue Eyes–Brown Eyes** In humans, the brown eye gene B is dominant and the blue eye gene b is recessive. This means that humans whose eye genes are BB , Bb , or bB have brown eyes and those with bb have blue eyes. The Punnett square at the right shows the results of eye colors for children of parents who each have one B gene and one b gene. What percentage of children will have brown eyes? What percentage will have blue eyes? Use the model $(0.5B + 0.5b)^2 = 0.25BB + 0.5Bb + 0.25bb$ to answer the question.

	B	b
B	BB	Bb
b	bB	bb

Algebra

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Review for Quiz 10-1, 2, 3

Hour _____

Use a vertical or horizontal format to add or subtract.

1) $(5x^2 - 2x + 4) + (-2x^2 + 3x - 1)$ 2) $(6n^2 + 4n + 6) - (5n^2 + n + 2)$

3) $(4n^2 - 6n + 5) - (8n^2 + n + 3)$ 4) $(3m^2 + 2m + 1) - (-2m^2 + 4m)$

5) $(5x^2 - 9) + (-3x^2 + 5x + 9)$ 6) $(n^2 - 2n) - (-5n^2 + 3n - 1)$

7) $(-2x^2 - 7x + 3) - (-5x^2 + 3x - 7)$ 8) $(x^3 + x^2 + x + 1) + (-x^2 - x - 1)$

Find the product.

9) $(2x)(5x - 1)$ 10) $(8m^2 - 4m + 1)(3m^2)$ 11) $(5a^2 + 3a - 7)(-2a^2)$

Use FOIL to find the product.

12) $(3z + 1)(z + 2)$

13) $(2x - 2)(x + 8)$


14) $(x - 2)(x - 3)$

15) $(5n + 3)(4n - 2)$

16) $(5x + 4)(3x - 2)$

17) $(4t + 3)(4t + 3)$

18) $(10n + 5)(3n - 2)$

 19) $(x^2 + 3x + 1)(x - 2)$

20) $(6 - x)(6 + x)$

21) $(2x + 7)(2x - 7)$

22) $(5x + 3)(5x - 3)$

Write the square of the binomial as a trinomial.

23) $(x + 8)^2$

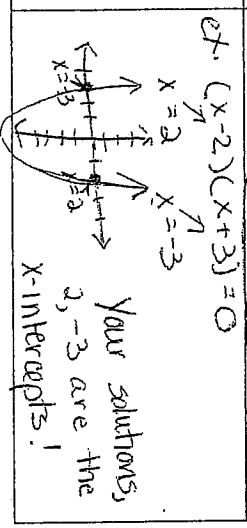
24) $(4m - 3)^2$

25) $(2k - 3)^2$

Algebra Chapter 10 Review

<p>① Polynomial in Standard Form</p>	<p>Leading Coefficient \downarrow Degree $2x^3 + 5x^2 - 4x + 7$ Constant term \leftarrow</p>	<p>Standard form means the terms are placed in order from largest degree to smallest degree.</p>
<p>② Types of Polynomials (classified by # of terms)</p>	<p>Terms monomial \rightarrow 1 term ($3x$) binomial \rightarrow 2 terms ($3x+2$) trinomial \rightarrow 3 terms ($4x^2+3x+2$)</p>	<p>Examples a) $x^2 + 2x - 5$ is a quadratic trinomial b) $4x^3 - 8x$ is a cubic binomial c) 6 is a constant monomial. d) $2x^4 - 7x^3 - 5x + 1$ is a quartic polynomial</p>
<p>③ Types of Polynomials (classified by degree)</p>	<p>Degree 0 \rightarrow constant 1 \rightarrow linear 2 \rightarrow quadratic 3 \rightarrow cubic 4 \rightarrow quartic</p>	<p>a) $(2x^2 + x - 5) + (x + x^2 + 6)$ $(2x^2 + x^2) + (x + x) + (-5 + 6)$ $3x^2 + 2x + 1$</p>
<p>④ Adding and subtracting Polynomials</p>	<p>To add or subtract two polynomials, add or subtract like terms.</p>	<p>* Adding a) $(x^2 - 4x^2) - 8 - 7x$ $(x^2 - 4x^2) - 8 - 7x$ $-3x^2 - 8 - 7x$ $-3x^2 - 7x - 8$ Standard form.</p>
	<p>* When you subtract the second polynomial, don't forget to subtract each term.</p>	

<p>5</p> <p>Multiplying <u>two</u> Binomials using FOIL</p>	<p>FOIL</p> <p>F i r s</p> <p>O u t e r</p> <p>I n e r</p> <p>L a g e</p>	<p>When you square a binomial, write the binomial twice and use FOIL.</p> <p>or</p> $(3x+4)(3x+4)$ $3x^2 + 15x + 4x + 16$ $3x^2 + 19x + 16$
<p>6</p> <p>Multiplying Polynomials of any size.</p>	<p>Use the distributive property. Remember each term of one polynomial must be multiplied by each term of the other polynomial.</p>	<p>or</p> $(3x-4)(5+3x-x^2)$ $15x + 9x^2 - 3x^3 - 20 - 12x + 4x^2$ <p>After you distribute, combine like terms.</p>
<p>7</p> <p>Special Product Patterns</p> <p>Sum and difference pattern</p>	<p>$(a+b)(a-b) = a^2 - b^2$</p> <p>The product of the sum and difference pattern has <u>no middle term</u>.</p>	<p>or</p> $(9x^2+4x^2) + (15x-12x) - 20$ $-3x^3 + 13x^2 + 3x - 20$ <p>↑</p> <p>Be sure the final answer is in standard form.</p> <p>or</p> $(3x+5)(3x-5)$ $9x^2 - 25$

<p>8</p> <p>Factored Form</p>	<p>A polynomial is in factored form if it is written as the product of two or more linear factors.</p>	<p>Standard Form: $2x^2 + 7x - 15 = 0$ * Factored Form: $(2x-3)(x+5) = 0$</p>
<p>9</p> <p>Solving Polynomial Equations in factored form</p>	<p><u>Zero-Product Property:</u> The product of two factors is zero only if one of the factors is zero.</p> <p><u>Repeated factors:</u> If an equation has a repeated factor, you only need to set the factor to zero one time because the answer would be the same.</p> <p><u>Solving a factored cubic equation:</u> Set <u>each</u> factor equal to zero.</p>	<p>Solve $(x-2)(x+3) = 0$ $x-2=0$ $x+3=0$ $x=2$ $x=-3$ <u>Solution</u> $x = 2, -3$</p> <p><u>Solve</u> $(x+5)^2 = 0$ $x+5 = 0$ <u>Solution</u> $x = -5$ There is only one solution for this repeated factor.</p> <p><u>Solve</u> $(2x+1)(x+3)(x-1) = 0$ $2x+1=0$ $x+3=0$ $x-1=0$ $2x=-1$ $x=-3$ $x=1$ $x=-\frac{1}{2}$ <u>Solutions</u> $x = -\frac{1}{2}, -3, 1$</p>
<p>10</p> <p>Relating x-intercepts and factors.</p>	<p>When you solve a factor of a polynomial for zero, you are actually finding the x-intercepts of the equation.</p>	<p><u>Solve</u> $(x-2)(x+3) = 0$ $x=2$ $x=-3$ Your solutions, 2, -3 are the x-intercepts!</p> 

Factoring $x^2 + bx + c = (x+p)(x+q)$

* Remember: $p+q=b$
 $(p)(q)=c$

11 Factoring when both b and c are positive.

$x^2 + 3x + 2$
 $b \rightarrow 3, c \rightarrow 2$
 $(x+1)(x+2)$

Find factors of c
 $(1, 2) \rightarrow 1+2=3$
 $(2, 1) \rightarrow 2+1=3$

Check by FOIL method.
 $(x+1)(x+2)$
 $x^2 + 2x + 1x + 2$
 $x^2 + 3x + 2 \rightarrow$ Same as original trinomial, so factoring is correct.

12 Factoring when b is negative and c is positive.

$x^2 - 5x + 6$
 $b \rightarrow -5, c \rightarrow 6$
 $(x-2)(x-3)$

Find factors of c
 $(1, 6), (-1, 6), (2, 3), (-2, 3)$
 $(-2, 3) \rightarrow -2+3=1$
 $(-3, 2) \rightarrow -3+2=-1$

Check by FOIL method
 $(x-2)(x-3)$
 $x^2 - 3x - 2x + 6$
 $x^2 - 5x + 6 \rightarrow$ Same as original trinomial, so factoring is correct!

13 Factoring when both b and c are negative.

$x^2 - 2x - 8$
 $b \rightarrow -2, c \rightarrow -8$
 $(x-4)(x+2)$

Find factors of c
 $(-1, 8), (-2, 4), (-4, 2), (-8, 1)$
 $(-4, 2) \rightarrow -4+2=-2$

Check by FOIL method
 $(x-4)(x+2)$
 $x^2 + 2x - 4x - 8$
 $x^2 - 2x - 8 \rightarrow$ Same as original trinomial, so factoring is correct.

14 Discriminant $b^2 - 4ac$

The discriminant must be a perfect square in order to factor a quadratic trinomial.

$ax^2 + bx + c$

1 Can $x^2 + 3x - 4$ be factored?
 $b^2 - 4ac = 3^2 - 4(1)(-4) = 9 + 16 = 25$
* Yes, because 25 is a perfect square.

2 Can $x^2 + 3x - 6$ be factored?
 $b^2 - 4ac = 3^2 - 4(1)(-6) = 9 + 24 = 33$
* No, because 33 is not a perfect square.